

# Horton Park Primary School

## Maths Calculation Policy



*September 2015*

**Reviewed** – September 2016


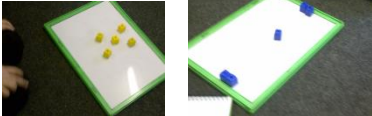

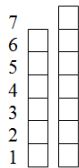
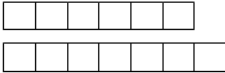
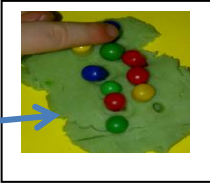


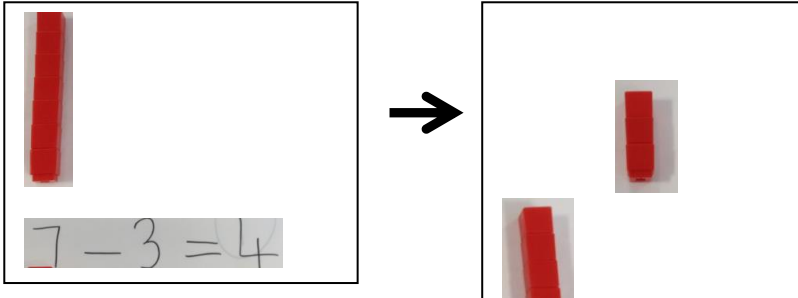



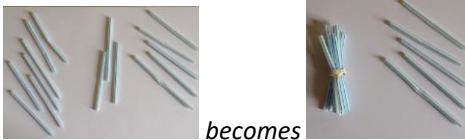
Horton Park Primary  
We Learn to Succeed

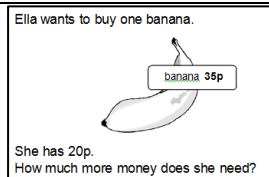
## **Section: 1**

# Subtraction & Addition

This is the calculation policy for Horton Park Primary School (created in association with Sharon Day of SharonDayMaths Ltd.), ready for the Autumn term 2015, which lists the progression through subtraction and addition. YR, Y1 and Y2 are mostly working mentally (which means using concrete resources to build conceptual understanding of the operations). The signs and number sentences for addition and subtraction are introduced throughout year 1. During year 3 the formal written methods for subtraction and addition are introduced as the children are working with numbers which demand this. Mental mathematics runs throughout with the children being trained to study the numbers before they start to decide on the most efficient method for working it out. The words in standard font are taken from the NC programme of study. Reference should be made to this document when planning to ensure that other skills from other domains that feed into calculating are utilised i.e. the domain for Number and Place Value. *The words in italics are guidance put together by the school to support teachers with the delivery of the policy.*

Year	subtraction	addition
YR	<p>Ensure children:</p> <ul style="list-style-type: none"> <li>are able to subitise (up to six items) firstly in recognised patterns then moving to random arrangements</li> </ul>  <ul style="list-style-type: none"> <li>realise that when the same amount is rearranged it is the same number and that an amount only changes its quantity when more is added or some is taken away (<i>including the game bunny ears – ‘finger gnosis’</i>)</li> </ul>  <ul style="list-style-type: none"> <li>can respond appropriately to ‘screened’ amounts and they know when an amount is covered that it is still there</li> <li>can use their knowledge of one more/less to say what the total will be if an extra one is put on top of the ‘screen’ or if one is taken from the screened amount moving to two more/less</li> </ul>  <div data-bbox="1352 879 1928 1016" style="border: 1px solid black; padding: 5px; margin-top: 10px;"> <p><i>Having number tracks vertically on display and for children to use to count up and down on helps with the concept of more and less.</i></p> </div> <p>ELG 11: Children count reliably with numbers from one to 20, place them in order and say which number is one more or one less than a given number. Using quantities and objects, they add and subtract two single-digit numbers (<i>amounts</i>) and count on or back to find the answer.</p> <div style="display: flex; align-items: flex-start;"> <div style="margin-right: 20px;">   </div> <div style="border: 1px solid black; padding: 5px; margin-right: 20px;"> <p><i>Using Unifix towers, or similar, compare amounts ‘Seven is one more than six so that means that six is one less than seven.’</i></p> </div> <div style="border: 1px solid black; padding: 5px; margin-right: 20px;"> <p><i>Play dough is a good experience for one less as the equipment taken away from the dough leaves an imprint:</i></p> </div> <div>  </div> </div>	
Year 1	<p>They should discuss and solve problems in familiar practical contexts, including using quantities. Problems should include the terms put together, add, altogether, total, take away, difference between, more than and less than so that pupils develop the concept of addition and subtraction and are enabled to use these operations flexibly. <i>The use of vertical number tracks supports with children understanding numbers increasing and decreasing.</i></p>	
	read, write and interpret mathematical statements involving subtraction (-) and	read, write and interpret mathematical statements involving addition (+)

	<p>equals (=) signs (using numbers from 0 to 20)</p> <p><i>Understand the subtraction sign such as seven can be built with 3 and 4 so 7 subtract 3 is 4 and 7 subtract 4 is 3 (show this in stages):</i></p> <div></div> <p>Solve one-step problems that involve subtraction using concrete objects and pictorial representations, and missing number problems such as <math>7 = \square - 9</math>. <i>i.e. There are fifteen cubes in this box. I am taking out three of the cubes. How many cubes are left in the box?</i> <i>i.e. There are seven bricks in the box. How many more bricks must we put in the box to make fifteen bricks altogether?</i> <i>Can count verbally backwards from a given number. Understand that when subtracting the amount becomes smaller. The following shows a number track and towers of cubes horizontally – also provide vertical experiences of the same idea.</i></p> <div></div> <p><i>Experience counting on from the smallest to largest number. Also experience 'seeing' how much the distance is without counting in ones (Subitising). Make links to solving "How many more /fewer?" type questions.</i></p>	<p>and equals (=) signs (using numbers from 0 to 20)</p> <p><i>Work on number facts i.e. bonds to make all numbers up to, and including, ten:</i></p> <div></div> <p><math>5=2+2+1</math></p> <div></div> <p>Solve one-step problems that involve addition, using concrete objects and pictorial representations, and missing number problems such as <math>17 = \square + 9</math>. <i>i.e. There are eight cups on the table. Put four more cups on the table. How many cups are on the table now?</i></p> <p>Add and subtract one-digit and two-digit numbers to 20, including zero</p> <p><math>7 + 3 + 5 = 15</math></p> <div></div>
Year 2	<p>Solve problems with addition and subtraction:</p> <ul style="list-style-type: none"><li>• using concrete objects and pictorial representations, including those involving numbers, quantities and measures</li><li>• applying their increasing knowledge of mental and written methods</li><li>• <i>include playing the 'swap shop' game (see appendix) with the straw bundles and then base 10 resources to support with using them to understand addition and subtraction written methods in year 3</i></li><li>• <i>problems including difference/distance between/more than/less than such as with: 'How many more red cubes are there <b>than</b> blue cubes?'</i></li></ul>	

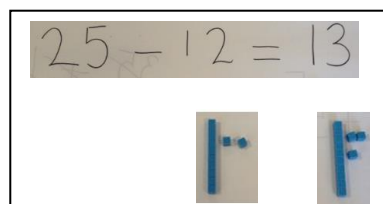
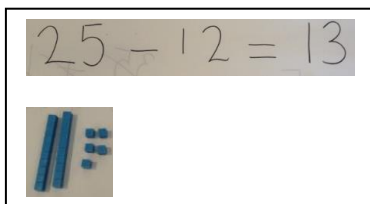
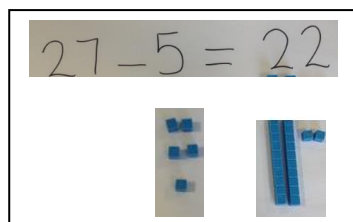
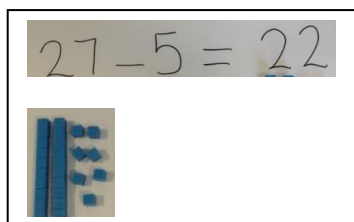


There are 4 fewer boys than girls in Mr Hill's class. There are 18 girls. How many boys are there in Mr Hill's class?

Recording addition and subtraction in columns supports place value and prepares for efficient written methods with larger numbers. (Where largest number is up to 100 – or beyond if appropriate to the child.)

subtract numbers using concrete objects, pictorial representations, and mentally, including:

- ☐ a two-digit number and ones
- ☐ a two-digit number and tens
- ☐ two two-digit numbers



And in a variety of contexts i.e. using coins:

Amy has these coins in her purse.



How much is in Amy's purse?

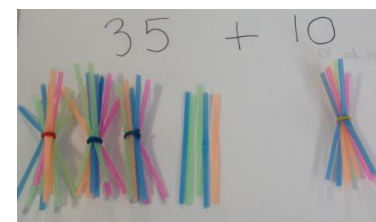
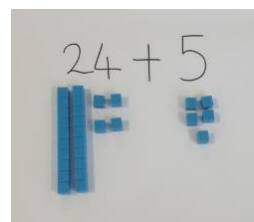
Amy spends 10p. How much does she have left?

There were 24 biscuits in a packet. Jack put 7 of the biscuits on a plate.

How many biscuits were left in the packet?

add numbers using concrete objects, pictorial representations, and mentally, including:

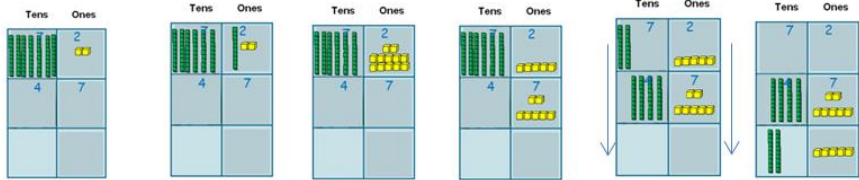
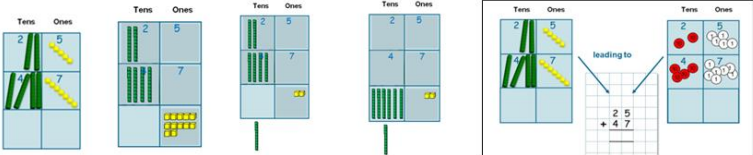

- ☐ a two-digit number and ones
- ☐ a two-digit number and tens
- ☐ two two-digit numbers
- ☐ adding three one-digit numbers

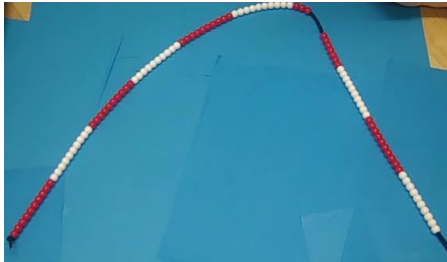
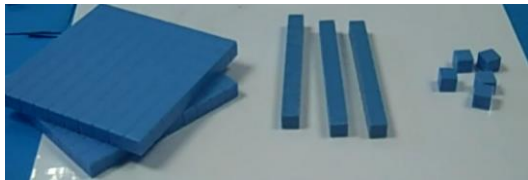
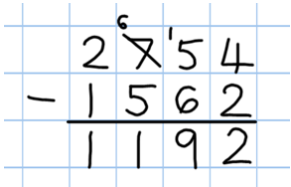
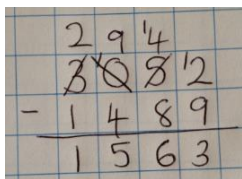
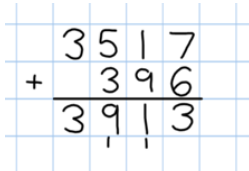
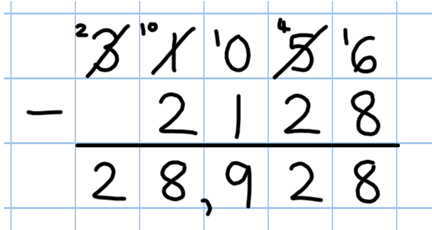
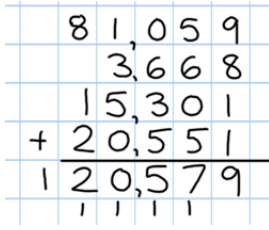


*Moving to recording the larger number with just numerals and building the smaller amount only to use as a model to see what happens when counting on 'in your head'.*



*Encourage children to rearrange amounts to use knowledge of bonds so the above could be rearranged as 6+4+3.*

<p><b>Year 3</b></p>	<p>Pupils use their understanding of place value and partitioning, and practise using columnar addition and subtraction with increasingly large numbers up to three digits to become fluent.</p> <p>Subtract numbers with up to three digits, using formal written method of columnar subtraction. <i>Use the NCETM models to support with understanding how to set it out: 72-47</i></p>  <p>Add numbers with up to three digits, using formal written method of columnar addition. <i>Use the NCETM models to support with understanding how to set it out: 25+47</i></p> 	
<p><b>A written method may be needed when digits in the smaller number are greater than in the larger number</b></p>	<p><i>Calculate 132 – 65 use the base 10 equipment to model the process step by step:</i></p> 	
<p><b>Ideas for working mentally</b></p>	<p>Pupils should be taught to add and subtract numbers mentally, including:</p> <ul style="list-style-type: none"> <li>a three-digit number and ones i.e.: 363+4 (count on and/or use knowledge of bonds of seven) 373+7 (use bonds of ten) 458+7 (count on and/or use bonds) 363-4 (count back and/or use knowledge of bonds) 567-7 (use knowledge of partitioning) 324-9 (use knowledge of subtracting ten and add on – adjust)</li> <li>a three-digit number and tens i.e.: 534+40 (count on from 534 in tens) 672-30 (count back from 672 in tens) 523 – 20 (partition/‘take out’ the tens)</li> <li>a three-digit number and hundreds i.e.: 457 +300 (use knowledge of four plus three with hundreds) 673 – 400 (use knowledge of six subtract four with hundreds)</li> </ul> <p>100 – 37 (as can be done mentally using knowledge of complements of 100)</p> <p>100 + 32 (as can be done mentally using knowledge of recombining)</p>	

	<p>Bead strings are a good model to use to see the effect of complements of numbers to 100 where there is value in the Units i.e. because <math>37+63=100</math> then <math>100-37=63</math>:</p> 	<p>Base 10 resources are good for children to conceptually understand this (and the clue is in the name: 'one hundred plus thirty-five is one hundred <b>and</b> thirty-five.')</p> 
<b>Year 4</b>	Pupils continue to practise both mental methods and columnar addition and subtraction with increasingly large numbers to aid fluency.	
	Subtract numbers with up to 4 digits using the formal written method of columnar addition where appropriate.	Add numbers with up to 4 digits using the efficient written method of columnar subtraction where appropriate.
<b>Examples of the types of numbers where a written method may be needed</b>	<p><math>2\ 754 - 1\ 562</math>:                      <math>3\ 052 - 1\ 489</math></p>  	<p><math>3\ 517 + 396</math>:</p>  <p>(Be aware that some children may be able to find the answer to the above example by adding 400 to 3517 and then adjusting by subtracting 4 in their head.)</p>
<b>Ideas for working mentally</b>	<p><math>1000 - 132</math> (this can be done mentally using complements of 100)  <math>2000 - 5</math> (this can be done by counting back the small number and/or using bonds of 10)</p>	<p><math>3000 + 567</math>      <math>3472 + 1111</math>      <math>3456 + 1000</math>      <math>5634 + 100</math>  <math>6743 + 10</math> (as all of these can be done mentally referring to place value)</p>
<b>UKS2</b>	Pupils practise using the formal written methods of columnar addition and subtraction with increasingly large numbers to aid fluency. (Pupils continue to use mental methods when the numbers allow for this.) Empty decimal places can be filled with zeroes to show the place value in each column. Pupils should say '6 tenths add 7 tenths' to reinforce place value. Children should be extended to include up to 3 decimal places.	
	Subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition).	Add whole numbers with more than 4 digits, including using formal written methods (columnar subtraction).
<b>Examples of the types of numbers where a written method may be needed</b>	<p>Example for layout of subtraction using decomposition:</p> 	<p>Adding several numbers using column method:</p> 



*Including decimal numbers:*

Line up the decimal points ↓	Line up the decimal points ↓
$\begin{array}{r} 76.3 \\ - 34.1 \\ \hline 42.2 \end{array}$	$\begin{array}{r} 4.321 \\ - 4.1 \\ \hline 0.221 \end{array}$

*Other examples:*

*Include measures such as 9.07km – 1 496m where converting will be needed*

*Include money such as £127.17 – £74.86*

*Other examples (which do not require 'carrying' but may still be better done*

*in a column because of the number of digits in the numbers):*

*63 141 + 3 756 becomes:*

$$\begin{array}{r} 63141 \\ + 3756 \\ \hline 66897 \end{array}$$

*(which do require 'carrying'):*

*27 424 + 9 694 becomes:*

$$\begin{array}{r} 27424 \\ + 9694 \\ \hline 37118 \\ \hline 111 \end{array}$$

*Include measures such as  
1.32km + 973m*

*Include money such as  
£17.17 + £14.86*

*Including decimal numbers:*

*For example: 56.39 + 18.61*

Line up the  
decimals like this:

$$\begin{array}{r} 56.39 \\ + 18.61 \\ \hline \end{array}$$

Then just add the  
numbers like normal:

$$\begin{array}{r} 56.39 \\ + 18.61 \\ \hline 75.00 \end{array}$$

# **WARNING!**

*If writing on squared paper (which would make sense to do as the SAT Arithmetic paper has squares to work out on) ensure that children are NOT taught to put the decimal point in a square. This can be confusing for some children if they are because they think that the decimal point is another 'place' rather than just a marker between the whole and decimal numbers. Instead place the dot on the line in between the Unit and tenth columns:*

~~$$\begin{array}{r} £23.59 \\ + £7.55 \\ \hline £31.14 \end{array}$$~~

~~$$\begin{array}{r} 7169.0 \\ - 372.5 \\ \hline 6796.5 \end{array}$$~~

$$\begin{array}{r} £23.59 \\ + £7.55 \\ \hline £31.14 \end{array}$$





<b>Ideas for working mentally</b>	<p>Subtract one point nine from two point seven.</p> <p>Subtract nought point one from two.</p> <p>What is thirty-one point nine subtract twenty-one point four?</p> <p>Calculate ten minus four point three five.</p> <p><math>12\ 462 - 2300 = 10\ 162</math></p>	<p>What is the sum of eight point five and eight point six?</p> <p>Add together nought point two, nought point four and nought point six.</p> <p>Mental questions including adding fractions and mixed numbers: Add together two and a half and three and a half and four and a half.</p> <p>Mental questions including more than one operation i.e.: Two metres of wire cost ninety pence. How much will three metres of wire cost?</p>
<b>Formal written methods taken from the National Curriculum (2014) appendix</b>	<div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>874 – 523 becomes</p> <math display="block">\begin{array}{r} 8\ 7\ 4 \\ -\ 5\ 2\ 3 \\ \hline 3\ 5\ 1 \end{array}</math> <p>Answer: 351</p> </div> <div style="text-align: center;"> <p>932 – 457 becomes</p> <math display="block">\begin{array}{r} \overset{8}{9}\ \overset{12}{3}\ \overset{1}{2} \\ -\ 4\ 5\ 7 \\ \hline 4\ 7\ 5 \end{array}</math> <p>Answer: 475</p> </div> </div>	<div style="text-align: center;"> <p>789 + 642 becomes</p> <math display="block">\begin{array}{r} 7\ 8\ 9 \\ +\ 6\ 4\ 2 \\ \hline 1\ 4\ 3\ 1 \\ \hline 1\ 1 \end{array}</math> <p>Answer: 1431</p> </div>




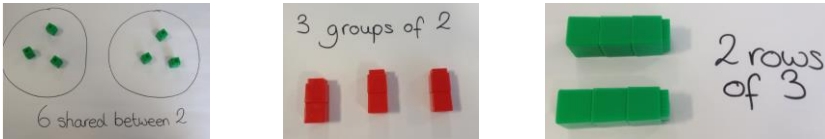






Horton Park Primary  
We Learn to Succeed

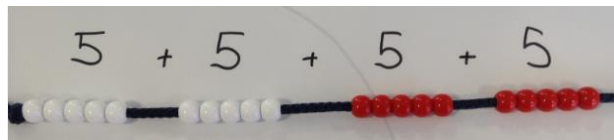
## **Section: 2**

# Division & Multiplication

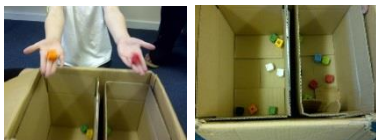
This is the calculation policy for Horton Park Primary School (created in association with Sharon Day of SharonDayMaths Ltd.), ready for the Autumn term 2015, which lists the progression through division and multiplication. YR, Y1 and Y2 and Y3 are mostly working mentally (which means using concrete resources to build conceptual understanding of the operations and then using growing knowledge of times table facts). The signs and number sentences for division and multiplication are introduced throughout year 2. During year 4 the formal written methods for multiplication and division are introduced as the children are working with numbers which demand this. Long multiplication is introduced in year 5 and long division, should it be required, is introduced in year 6. Mental mathematics runs throughout with the children being trained to study the numbers before they start to decide on the most efficient method for working it out. The words in standard font are taken from the NC programme of study. Reference should be made to this document when planning to ensure that other skills from other domains that feed into calculating are utilised i.e. the domain for Number and Place Value. *The words in italics are guidance put together by the school to support teachers with the delivery of the policy.*

Year	division	multiplication
FS	<p>ELG 11: Children solve problems using doubling, halving and sharing.</p>  <p>Provide opportunities to have experience of recognising where items are organised into equal groups and then putting together equal groups of items in various areas of provision.</p>  <div data-bbox="1178 686 1830 847">  <p>'How many bags of apples with five in each bag can you make?' 'I can make two bags of five apples.'</p> </div>	
Year 1	<p>Through grouping and sharing small quantities, pupils should begin to understand multiplication and division; doubling numbers and quantities, and finding simple fractions of objects, numbers and quantities.</p>  	
	<p>Solve one-step problems involving division (<i>experiencing sharing and grouping</i>), calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher. <i>(No expectation for recording formally at this stage.)</i></p> <p>Share these pencils equally between Asif and Ben. How many pencils will each of them get?</p>  <p>How many children can have two squares each, from this chocolate bar?</p> 	<p>Solve one-step problems involving multiplication, calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher. <i>(No expectation for recording formally at this stage.)</i></p> <p>Count the eggs in this egg box.</p>  <p><i>It is promoted and then expected that the children will count in twos using two extended fingers to keep track of the count.</i></p>
Year 2	<p>Pupils solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division</p>	

facts, including problems in contexts. (i.e. division is 'grouping' only for calculating and 'sharing' by 2 is only referred to during halving activities)  
Pupils solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts. (ensure that division is 'grouping' for calculating and 'sharing' by 2 is only used during halving activities)



Four groups of five is written as  $5+5+5+5$  which is 'Five, four times' which is eventually written as  $5 \times 4$  as the first number in the calculation is the amount we know – the group being multiplied.

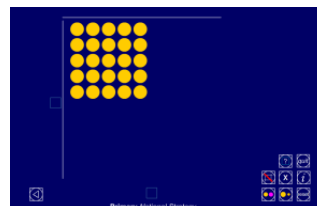


half of 14 is 7 (in each half):



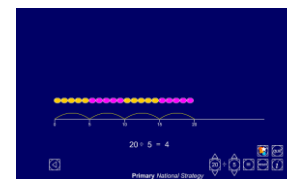
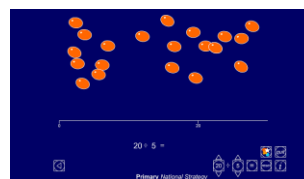
Half of 50 is 25 (in each half):

Array ITP:



This array shows:  $5 \times 5 = 25$ ;  
 $25 = 5 \times 5$ ;  $25 \div 5 = 5$ ; twenty-five in groups of five gives five groups of five.

Grouping ITP:



Calculate mathematical statements for division within the multiplication tables of 2, 5 and 10, writing them using the division ( $\div$ ) and equals (=) signs

(How many groups/sets/lots of two do we use to make fourteen?)...

'Fourteen divided by two is seven':  $14 \div 2 = 7$

(How many groups/sets/lots of five do we use to make forty-five?)...

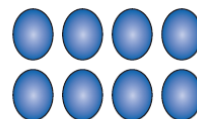
'Forty-five divided by five is nine':  $45 \div 5 = 9$

This is NOT 'sharing' – it is organising the dividend into GROUPS of the divisor.

Using the concept of grouping to support with learning tables facts:

Calculate mathematical statements for multiplication within the multiplication tables 2, 5, and 10, writing them using the multiplication ( $\times$ ) and equals (=) signs

When using an array read it from left to right, so this image is 'Two, four times' or ' $2+2+2+2$ ' or 'Two times by four' or 'Two multiplied by four':



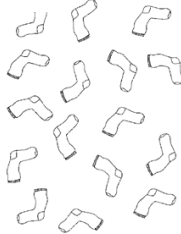









$$2 \times 4 = 8$$

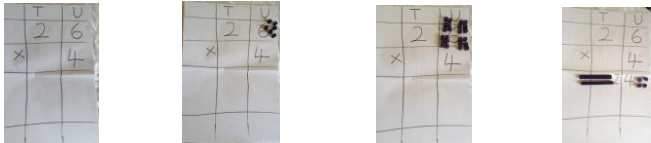


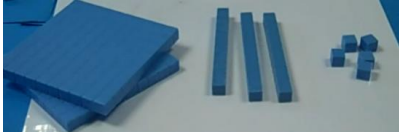
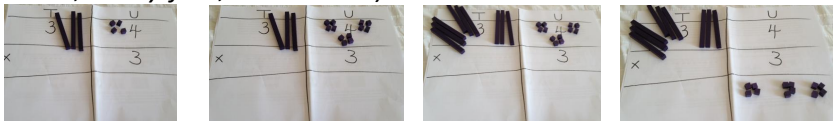
'Two times by seven is fourteen':  $2 \times 7 = 14$

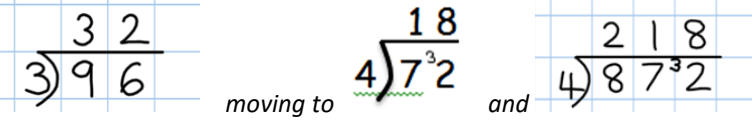



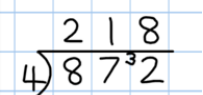
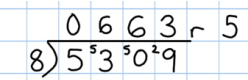

'Five multiplied by nine is forty-five':  $5 \times 9 = 45$

And in contexts:

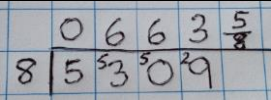
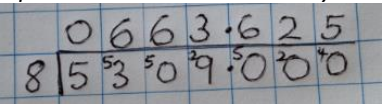
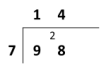
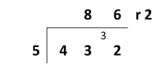
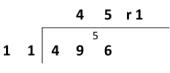



'How many two pence pieces do you need to make 20p?'

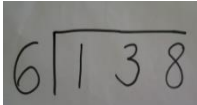
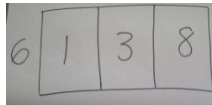
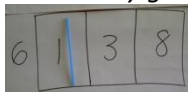
	<p>How many pairs of socks are there?</p>  <p><i>There are other questions that may demand the use of sharing such as 'halving and halving again' as with this:</i></p> <p>Four children share these shells. They each get the same number of shells.</p>  <p>How many shells does each child get?</p>	<p>There are 10 crayons in each box.</p>  <p>How many crayons are there altogether?</p>
<p><b>Year 3</b></p>	<p>Pupils develop <b>use of mental methods</b> for multiplication and division, starting with calculations of two-digit numbers by one-digit numbers and progressing to the efficient written methods of short multiplication and division (using the times tables of 2, 3, 4, 5, 8 and 10). <i>Explore arrays with the times tables they know to understand that once I know one fact I know more than one fact (i.e. the first image shows four</i></p> <div style="display: flex; justify-content: space-around; align-items: center;">   </div> <p><i>multiplied by six or 4+4+4+4+4+4 and the second image shows six multiplied four or 6+6+6+6 but they both answer twenty-four):</i> <math>4 \times 6 = 24</math>    <math>6 \times 4 = 24</math></p> <p><i>Mental methods will include:</i></p> <ul style="list-style-type: none"> <li><i>partitioning amounts in different ways using base 10 resources in response to being equally divisible by the above multiples i.e. 'Put sixty-eight into different arrangements so that each part of it is equally divisible by four.'</i></li> </ul> <div style="display: flex; justify-content: space-around;">      </div> <p><i>The children can begin to record findings after they have created a variety of responses with the concrete resources (manipulatives). Encourage them to work systematically to find all possibilities. i.e. 68=60+8, 68=40+20+8, etc.</i></p> <ul style="list-style-type: none"> <li><i>use of a (vertical or horizontal) number line/jottings to record the amount of groups (the divisor) counted up to that gets you to the amount being divided (the dividend)</i></li> </ul>	
<p>Divide two-digit numbers by a one-digit number</p> <p><i>The children are given plenty of practical work and are encouraged to use mental strategies and informal pencil and paper or whiteboard jottings to support, record and to explain their thinking.</i></p> <p><i>Children are taught to solve division calculations by using</i></p>	<p>Multiply two-digit numbers by a one-digit number</p> <p><i>This could start with expanded method and would look like:</i></p> <div style="font-family: monospace;">       26        X 4        ---        24    (show with base 10 resources where these products have come from)        80     </div>	

	<p>multiplication strategies e.g. calculate <math>18 \div 3</math> by counting on in multiples of three or by recalling tables facts this could be modelled by keeping track of the number of groups of three with fingers where each finger 'stands for' 3.. The link between division and counting on in groups of the divisor should be made. This then progresses to dividing larger two-digit numbers i.e. <math>68 \div 4</math> where the number 68 (built with ten sticks and unit cubes is partitioned into 40 and 28, so that both parts are divisible by the divisor).</p>	<p>104 (show with base 10 resources from above where this total has come from)</p>  <p>Build then multiply the unit value, placing it in the answer 'box'.</p>  <p>Build then multiply the tens value and place in the answer 'box'.</p>  <p>Find the total on the two products by using the addition method.</p>
<b>Examples easily calculated mentally</b>	<p><math>24 \div 4</math> (as this can be done mentally using known facts but could be laid out in the short division format to promote familiarity; continue to use arrays to understand the concept)  <i>'I know that <math>4 \times 6 = 24</math> so then <math>24 \div 4 = 6</math>'</i></p>	<p><math>5 \times 4</math> (as this can be done mentally using known facts; continue to use arrays to understand the concept)  <math>3 \times 10</math> (as this can be done mentally by using the learned effect of multiplying by ten – NOT 'adding a zero' - the number becomes ten times bigger)</p>
<b>Year 4</b>	<p>Pupils should practise to become fluent in the efficient written method of short multiplication for multiplying using multi-digit numbers, and short division with exact answers when dividing by a one-digit number (with all 12 times tables facts)</p>  <div> <p><b>Practising partitioning numbers in different ways, in response to investigating in the context of a variety of divisors, supports children with understanding division and multiplication i.e. 'Make the number 235 with base 10 resources. Now move the resources around to make different numbers that are equally divisible by 5.' After exploration the children can begin to record such as: <math>200 + 30 + 5</math>; <math>100 + 100 + 20 + 15</math>; <math>100 + 100 + 10 + 10 + 5</math>; etc. 'Now move the same amount around into multiples of 4. What do you notice?' <math>100 + 100 + 20 + 12</math> with 3 left over etc.</b></p> </div>	
	<p>Divide two-digit and three-digit numbers by a one-digit number using formal written layout  <i>In order to become familiar with the short division layout begin with numbers that do not have remainders moving to calculating with numbers that require one amount to be 'carried'. Demonstrate for all children without the concrete resources then if there are children who question the validity of the method regarding it linking to place value show this group of children how the method works in relation to place value using base ten resources (see the example at the end of this document):</i></p>	<p>Multiply two-digit and three-digit numbers by a one-digit number using formal written layout.  <i>The following uses the example of <math>34 \times 3</math> ('thirty-four multiplied by three'; 'thirty-four, three times'):</i></p>  <p>Build 'top number'; multiply the units then the tens; place the answer</p>

	 <p>moving to      and</p> <p><b>See at the end of the document for discussion on short division method as well as details on how base ten resources could be used to help with conceptual understanding</b></p>	 <p>for the units and 'carry';      place the answer for the tens and 'carry'.</p> <p><b>See at the end of the document for the above in more detail, with commentary.</b></p>
<b>Other examples</b>	<p>Calculate <math>56 \div 4</math>  <math>456 \div 4</math></p> <p>To ensure children grasp how the layout for short division works ask them to respond to 'rich and sophisticated' questions that demand reasoning, such as:          Write in the missing digit.          The answer does not have a remainder.</p> 	<p>Calculate <math>58 \times 6</math> (where they have to set it out vertically from this)</p> <p>To ensure children grasp how the layout for short multiplication works ask them to respond to 'rich and sophisticated' questions that demand reasoning, such as:          Write in the missing digit.</p> 
<b>Examples when a written method may not be needed</b>	<p><math>97 \div 100</math> (this can be done using knowledge of what happens to a number when divided by 10, 100, etc.)  <math>242 \div 2</math> (this can be done by halving)  <math>55 \div 5</math> (this can be done using known facts)</p>	<p><math>97 \times 100</math> (this can be done using knowledge of what happens to a number when multiplied by 10, 100, etc.)  <math>33 \times 2</math> (this can be done by doubling)  <math>3 \times 70</math> (this can be done by combining known facts with multiplying by ten)</p>
<b>Year 5</b>	<p>Pupils practise and extend their use of the formal written methods of short multiplication and short division. They apply all the multiplication tables and related division facts frequently, commit them to memory and use them confidently to make larger calculations.</p>	
	<p>Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context.</p>	<p>Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers.</p>
<b>examples for written</b>	<p>Start with amounts where the first digit in the dividend is larger than the divisor:</p>  <p>Moving to amounts where the first digit in the dividend is smaller than the divisor:</p>  <p>Express answers as fractions (here there is a remainder of five out of the eight being divided into it so the remainder is 'five out of eight'):</p>	<p>Conceptual understanding of long multiplication (using manipulatives):</p> <p>Short multiplication that requires 'carrying' (multiplying by a single digit number): i.e. <math>327 \times 4</math> and <math>3,652 \times 8</math></p> 



	 <p>Express answers as decimals by 'carrying' into the decimal columns:</p> 	
<b>examples for mental</b>	<p>Any calculations where the dividend is a multiple of the divisor, known facts can be used and 'carrying' does not have to occur i.e. <math>8,884 \div 4</math></p> <p>Write in the missing number:</p> $3400 \div \square\square = 100$ (use their knowledge of place value) <p>Divide nought point nine by one hundred. (move the digits two places to the right)</p>	<p>Where the calculation demands moving a number in response to place value i.e. <math>452 \times 1,000</math></p> <p>What is double fifteen point five?</p> <p>Write in the missing number:</p> $8 \times \square = 400$
<b>Year 6</b>	Pupils practise multiplication and division for larger numbers, using the formal written methods of short and long multiplication, and short and long division.	
<b>examples for mental</b>	<p>Divide thirty-one point five by ten</p> <p>Ten times a number is eighty-six. What is the number?</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;">             Circle the best estimate of the answer to  <math>72.34 \div 8.91</math>              6    7    8    9    10    11           </div>	<p>What is nought point eight multiplied by six?</p> <p>What must you multiply nought point seven by to get two point one?</p> <p>A bag of four oranges costs thirty seven pence. How much do twelve oranges cost? (understanding how to use knowledge of related multiplication tables i.e. here the 12 times table is three times the four times table so to solve this you just need to multiply 37 by 3.)</p>
<b>Final outcomes for short formal written methods</b> (where the number is being divided or multiplied by a single digit number)	<div> <div> <p>Short division</p> <p><math>98 \div 7</math> becomes</p>  <p>Answer: 14</p> </div> <div> <p><math>432 \div 5</math> becomes</p>  <p>Answer: 86 remainder 2</p> </div> <div> <p><math>496 \div 11</math> becomes</p>  <p>Answer: <math>45 \frac{1}{11}</math></p> </div> </div> <p>The answers to short division, where the dividend cannot be divided equally by the divisor, can be shown as a remainder as well as fraction. Showing the remainder as a fraction is easy as we are just writing the remainder at the top of the fraction (numerator) and the divisor at the bottom of the fraction (denominator). 'We had one left over and we were dividing it by eleven so the remainder is written as one out of eleven'. It is also possible to use the short division method where the divisor is a larger two-digit number thus making the long division method unnecessary – the answer can be written as a decimal. The quotient can be expressed in different ways depending on context of how the context is expecting the answer)</p>	
	<p>Short multiplication</p> <div> <div> <p><math>24 \times 6</math> becomes</p>  <p>Answer: 144</p> </div> <div> <p><math>342 \times 7</math> becomes</p>  <p>Answer: 2394</p> </div> <div> <p><math>2741 \times 6</math> becomes</p>  <p>Answer: 16 446</p> </div> </div> <p>When teaching short multiplication we are working from the right as with addition and subtraction methods shown in columns. To support children with understanding about 'carrying along' where the product is a two-digit numbers use base 10 resources to model the amount that has been made (this builds on the formal method they will have learned for addition). So, in the first example when we calculate that six fours is twenty-four (hopefully using known facts) then we build the twenty-four displaying the 4 units in the Units column and the 2 tens carried over to the tens column. This is then combined with the product of six twenties to make 14 tens which is then recombined as one hundred flat and four ten sticks.</p>	

<p><b>Final outcomes for long formal written methods</b> (where the number is being divided or multiplied by a two digit number which is greater than 12)</p>	<div><p><b>Long division</b></p><div><div><p>432 ÷ 15 becomes</p><div><div><div><div>2</div><div>8</div><div></div></div><div><div>1</div><div>5</div><div></div></div><div><div>4</div><div>3</div><div>2</div></div><div><div>3</div><div>0</div><div>0</div></div><div><div>1</div><div>3</div><div>2</div></div><div><div>1</div><div>2</div><div>0</div></div><div><div>1</div><div>2</div><div></div></div></div></div><p>Answer: 28 remainder 12</p></div><div><div><p>432 ÷ 15 becomes</p><div><div><div><div>2</div><div>8</div><div></div></div><div><div>1</div><div>5</div><div></div></div><div><div>4</div><div>3</div><div>2</div></div><div><div>3</div><div>0</div><div>0</div></div><div><div>1</div><div>3</div><div>2</div></div><div><div>1</div><div>2</div><div>0</div></div><div><div>1</div><div>2</div><div></div></div></div></div><p>15×20</p><p>15×8</p><p><math>\frac{12}{15} = \frac{4}{5}</math></p><p>Answer: 28 <math>\frac{4}{5}</math></p></div><div><div><p>432 ÷ 15 becomes</p><div><div><div><div>2</div><div>8</div><div></div></div><div><div>1</div><div>5</div><div></div></div><div><div>4</div><div>3</div><div>2</div></div><div><div>3</div><div>0</div><div>0</div></div><div><div>1</div><div>3</div><div>2</div></div><div><div>1</div><div>2</div><div>0</div></div><div><div>1</div><div>2</div><div>0</div></div><div><div>1</div><div>2</div><div>0</div></div><div><div>1</div><div>2</div><div>0</div></div></div></div><p>Answer: 28.8</p></div></div></div><p>Long division can be done two ways and both ways have their reasons (and again the quotient can be expressed in different ways depending on context of how the context is expecting the answer):</p><div><div>1) We think of the number we are dividing (the dividend) as the full place value that they have (see the first two examples below – the second uses jottings to keep track of how many groups of the divisor have been used).</div><div>2) We think of the number we are dividing (the dividend) as if they are separate two-digit numbers.</div></div><p>Teach one of these versions to your class and any children still struggling with the version you have chosen after a while teach the other version as that may be the one that makes the most sense to them.</p></div></div>	<div><p><b>Long multiplication</b></p><div><div><p>24 × 16 becomes</p><div><div><div><div>2</div><div>4</div><div></div></div><div><div>×</div><div>1</div><div>6</div></div><div><div>2</div><div>4</div><div>0</div></div><div><div>1</div><div>4</div><div>4</div></div><div><div>3</div><div>8</div><div>4</div></div></div></div><p>Answer: 384</p></div><div><div><p>124 × 26 becomes</p><div><div><div><div>1</div><div>2</div><div>4</div></div><div><div>×</div><div>2</div><div>6</div></div><div><div>2</div><div>4</div><div>8</div><div>0</div></div><div><div>7</div><div>4</div><div>4</div></div><div><div>3</div><div>2</div><div>2</div><div>4</div></div></div></div><p>Answer: 3224</p></div><div><div><p>124 × 26 becomes</p><div><div><div><div>1</div><div>2</div><div>4</div></div><div><div>×</div><div>2</div><div>6</div></div><div><div>7</div><div>4</div><div>4</div></div><div><div>2</div><div>4</div><div>8</div><div>0</div></div><div><div>3</div><div>2</div><div>2</div><div>4</div></div></div></div><p>Answer: 3224</p></div></div></div><p>Long multiplication can be done two ways and both ways have their reasons:</p><div><div>1) Starting by multiplying the top number by the unit of the second number down builds on where the children start when they use the method for short multiplication.</div><div>2) Starting by multiplying the top number by the tens of the second number more closely matches what we do with grid method.</div></div><p>Teach one of these versions to your class and any children still struggling with the version you have chosen after a while teach the other version as that may be the one that makes the most sense to them.</p></div></div>
<p><b>MORE ABOUT SHORT DIVISION LAYOUT</b></p>	<p>For many teachers the short and long division formal method is problematic. It is a useful and efficient way of dividing as it is a quick method however some teachers feel an aversion to it as it can be learned as a trick with no understanding. Ironically it seems to be that children with a poorer understanding of place value pick the method up quicker, as children with good place value will often question how it works rather than just accept it as a ‘trick’. There are ways to attempt to link place value and models to the method and below is a series of images to attempt to illustrate these. One way uses bundles and refers to the digits in the dividend as individual digits and the second way uses base ten resources with an attempt to link the method to place value. I advise that you demonstrate the method to the majority of children without concrete resources initially then use the concrete resources in a guided session for children who do not acquire the method readily or who are questioning how it works in response to place value.</p> <p><b>The digits can be separated should it be required, but it does not have to be drawn in this way:</b></p> <div><div></div><div></div></div> <p>So for this calculation: draw a grid with the digits separated:</p> <p>Using bundles of straws (in tens) and single straws begin to work through it a section at a time: ‘How many groups of sixes can you get out of 1?’ ‘None.’:</p> <div></div> <p>‘So move the digit not used across to the next column and then build the new number (which is now thought of as thirteen) 13 with the</p>	

straws' (one ten and three units):



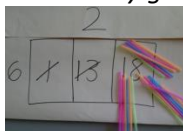
'How many groups of six can you get out of thirteen?' 'Two groups of six with one left over (remaining)':



'Carry the remaining digit over to the next section and then build the new number':



'How many groups of six can you make with eighteen?' 'Three groups of six':



'So the answer to one hundred and thirty-eight divided by six is twenty-three groups of six':



**The above could also be demonstrated using 'Base Ten' equipment which takes more account of the place value as follows. Use this for children who need to know how it works. Do not bother with this for children who are able to do the method 'as a trick' and are not questioning how it works unless you feel they would benefit from it. The important principle here is that as you divide in each column you make groups of the divisor multiplied by the value of the column so, if you are dividing 8 ones into groups of 2 then you would describe it as 'Eight ones put into groups of two ones is four groups of two ones.' You wouldn't just say 'Eight divided by two is four'. So if you were in the Tens column and it contained eight tens (80) you would say: 'Eight tens put into groups of two tens are four groups of two tens.' Hopefully the images below will help to clarify how to describe what is happening:**

$$6 \overline{) 138}$$

So for this calculation:



again draw a grid with the digits separated if you require it:

Using base 10 resources begin to work through it a section at a time:

'Can I make a **group of six 'hundreds'** from this model?' 'No because there is only one 'hundred.'':



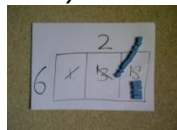
'So move the digit not used across and then build the new number (which is now thought of as **thirteen tens** because it is in the tens column) with ten sticks':



'Can I make any **groups of six tens**?' 'Yes. Two **groups of six tens** with one ten stick left over (remaining)'



'Carry the remaining digit over to the next section and then build the new number':



'How many **groups of six 'ones/units'** can you make with eighteen ones/units?' 'Three **groups of six 'ones/units'**':



'So the answer to one hundred and thirty-eight divided by six is twenty-three **groups of six**':

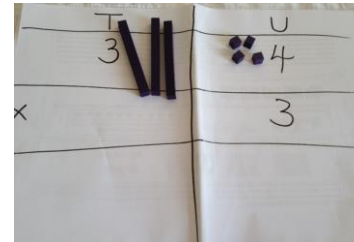
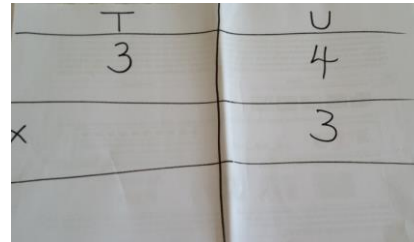
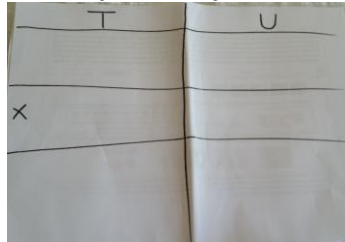
$$23 \overline{) 138}$$

# **Multiplication**

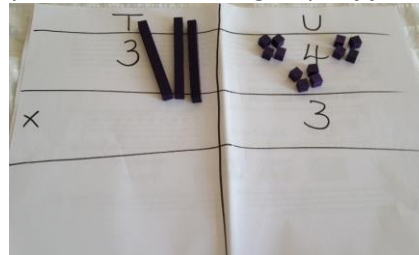
This demonstrates how the written method of short multiplication can be taught to children with conceptual understanding related to

**method in  
more detail**

place value. The following uses the example of  $34 \times 3$  ('thirty-four multiplied by three'; 'thirty-four, three times'):  
Draw a grid labeled with tens and ones and then build the number being multiplied (called the multiplicand) which is usually the larger amount of the two for ease:



Multiply the amount in the ones/Units column by the multiplier (the multiplier is the 'bossy' number and says 'I want three groups of four not just one group of four!') and be describing that you now have three groups of four as here we are multiplying 4 by 3:

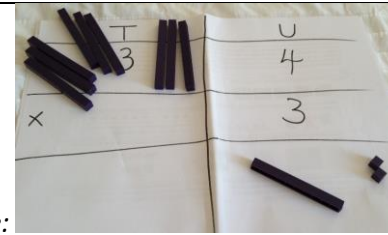


Do the same to the amount in the Tens column and build the product here (30, three times):



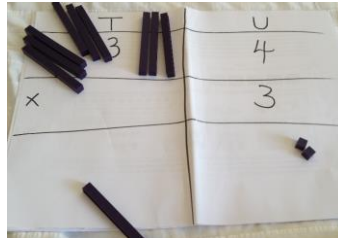
Move the product of the two Units into the Units answer box:





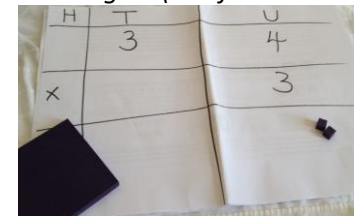
If that product exceeds 9 then it will need to be reorganised in relation to its place value:

and then



'carried' over:

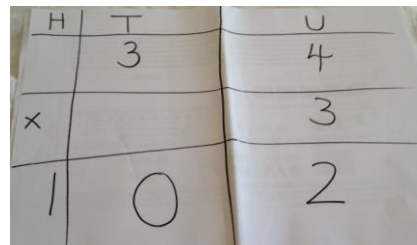
Combine the product for the Tens column with the carried amount and consider if it needs to be 'carried' again (i.e. if the total of the



carried amount and the product exceeds nine of them):



Then remove the practical apparatus:



Children should be able to move to creating this without the use of the concrete resources quite quickly once they have understood conceptually what is happening and how the method works.

